Random sampling locations for comparing a mean with a fixed threshold (parametric)

Summary

This report summarizes the sampling design used, associated statistical assumptions, as well as general guidelines for conducting post-sampling data analysis. Sampling plan components presented here include how many sampling locations to choose and where within the sampling area to collect those samples. The type of medium to sample (i.e., soil, groundwater, etc.) and how to analyze the samples (in-situ, fixed laboratory, etc.) are addressed in other sections of the sampling plan.

The following table summarizes the sampling design developed. A figure that shows sampling locations in the field and a table that lists sampling location coordinates are also provided below.

SUMMARY OF	SAMPLING DESIGN
Primary Objective of Design	Compare a site mean to a fixed threshold
Type of Sampling Design	Parametric
Sample Placement (Location) in the Field	Simple random sampling
Working (Null) Hypothesis	The mean value at the site exceeds the threshold
Formula for calculating number of sampling locations	Student's t-test
Calculated total number of samples	4
Number of samples on map ^a	42
Number of selected sample areas b	2
Specified sampling area ^c	188054.34 m ²
Total cost of sampling ^d	\$3,000.00

^a This number may differ from the calculated number because of 1) grid edge effects, 2) adding judgment samples, or 3) selecting or unselecting sample areas.

^b The number of selected sample areas is the number of colored areas on the map of the site. These sample areas contain the locations where samples are collected.

^c The sampling area is the total surface area of the selected colored sample areas on the map of the site.

^d Including measurement analyses and fixed overhead costs. See the Cost of Sampling section for an explanation of the costs presented here.



	Area: Area 1								
X Coord	Y Coord	Label	Value	Туре	Historical				
679133.4290	3083306.3130	J-01S	1200	Manual	Т				
679104.2450	3083223.2620	J-02S	7690	Manual	Т				
679155.0740	3083294.6960	J-03S	2250	Manual	Т				
679171.2970	3083289.7960	J-04S	747	Manual	Т				
679225.8560	3083359.9740	J-05S	959	Manual	Т				
679164.8060	3083214.7100	J-06S	6880	Manual	Т				
679242.7260	3083326.5280	J-07S	11400	Manual	Т				
679181.2750	3083178.2880	J-08S	10900	Manual	Т				
679213.7730	3083224.9730	J-09S	858	Manual	Т				
679280.5440	3083305.6810	J-10S	1090	Manual	Т				
679268.7700	3083200.3260	J-11S	1110	Manual	Т				
679301.1600	3083254.0340	J-12S	748	Manual	Т				

Area: Area 3							
X Coord	Y Coord	Label	Value	Туре	Historical		
679149.4920	3082933.0980	J-13S	5140	Manual	Т		
679279.6830	3083075.4290	J-14S	917	Manual	Т		

679261.0980 3083016.3510 J-15S 5880 Manual T 679222.6340 3082840.1720 J-16S 3640 Manual T 679293.5600 3082950.4980 J-17S 1130 Manual T 679360.5700 3083026.4980 J-18S 3510 Manual T 679343.5810 3082969.5980 J-19S 1760 Manual T 679382.8640 3083009.1130 J-20S 915 Manual T 679335.0020 3082941.1720 J-21S 648 Manual T 679252.7130 3082781.0290 J-22S 1960 Manual T 679297.0010 3082840.6970 J-23S 4180 Manual T 679394.8070 3082549.7640 J-24S 790 Manual T 679169.0760 3082537.3510 J-26S 2800 Manual T 679329.4380 3082711.0960 J-29S 3630 Manual T 679374.4420 30828						
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	679524.3310	3082886.8990	J-40S	1495	Manual	Т
679328.5397 3082643.5206 0 Random	679560.6070	3082897.2580	J-41S	2480	Manual	Т
	679328.5397	3082643.5206		0	Random	

Primary Sampling Objective

The primary purpose of sampling at this site is to compare a mean value with a fixed threshold. The working hypothesis (or 'null' hypothesis) is that the mean value at the site is equal to or exceeds the threshold. The alternative hypothesis is that the mean value is less than the threshold. VSP calculates the number of samples required to reject the null hypothesis in favor of the alternative hypothesis, given a selected sampling approach and inputs to the associated equation.

Selected Sampling Approach

A parametric random sampling approach was used to determine the number of samples and to specify sampling locations. A parametric formula was chosen because the conceptual model and historical information (e.g., historical data from this site or a very similar site) indicate that parametric assumptions are reasonable. These assumptions will be examined in post-sampling data analysis.

Both parametric and non-parametric approaches rely on assumptions about the population. However, non-parametric approaches typically require fewer assumptions and allow for more uncertainty about the statistical distribution of values at the site. The trade-off is that if the parametric assumptions are valid, the required number of samples is usually less than the number of samples required by non-parametric approaches.

Locating the sample points randomly provides data that are separated by many distances, whereas systematic samples

are all equidistant apart. Therefore, random sampling provides more information about the spatial structure of the potential contamination than systematic sampling does. As with systematic sampling, random sampling also provides information regarding the mean value, but there is the possibility that areas of the site will not be represented with the same frequency as if uniform grid sampling were performed.

Number of Total Samples: Calculation Equation and Inputs

The equation used to calculate the number of samples is based on a Student's t-test. For this site, the null hypothesis is rejected in favor of the alternative hypothesis if the sample mean is sufficiently smaller than the threshold. The number of samples to collect is calculated so that 1) there will be a high probability $(1-\beta)$ of rejecting the null hypothesis if the alternative hypothesis is true and 2) a low probability (α) of rejecting the null hypothesis is true.

The formula used to calculate the number of samples is:

$$n = \frac{S^2}{\Delta^2} \left(Z_{1-\alpha} + Z_{1-\beta} \right)^2 + 0.5 Z_{1-\alpha}^2$$

where

n is the number of samples,

S is the estimated standard deviation of the measured values including analytical error,

 Δ is the width of the gray region,

 α is the acceptable probability of incorrectly concluding the site mean is less than the threshold,

is the acceptable probability of incorrectly concluding the site mean exceeds the threshold,

is the value of the standard normal distribution such that the proportion of the distribution less than $Z_{1-\alpha}$ is 1- α , is the value of the standard normal distribution such that the proportion of the distribution less than $Z_{1-\alpha}$ is 1- α .

The values of these inputs that result in the calculated number of sampling locations are:

Analysta	_	Parameter						
Analyte	"	S Δ α β $Z_{1-\alpha}$ α					Z_{1-β} b	
	4	3329.4	6513.2	0.05	0.1	1.64485	1.28155	

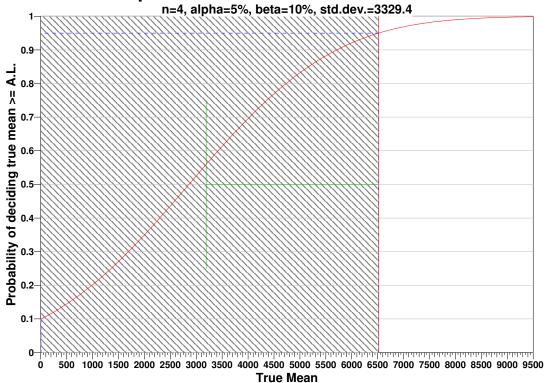
^a This value is automatically calculated by VSP based upon the user defined value of α .

b This value is automatically calculated by VSP based upon the user defined value of β.

The following figure is a performance goal diagram, described in EPA's QA/G-4 guidance (EPA, 2000). It shows the probability of concluding the sample area is dirty on the vertical axis versus a range of possible true mean values for the site on the horizontal axis. This graph contains all of the inputs to the number of samples equation and pictorially represents the calculation.

The red vertical line is shown at the threshold (action limit) on the horizontal axis. The width of the gray shaded area is equal to Δ ; the upper horizontal dashed blue line is positioned at 1- α on the vertical axis; the lower horizontal dashed blue line is positioned at β on the vertical axis. The vertical green line is positioned at one standard deviation below the threshold. The shape of the red curve corresponds to the estimates of variability. The calculated number of samples results in the curve that passes through the lower bound of Δ at β and the upper bound of Δ at 1- α . If any of the inputs change, the number of samples that result in the correct curve changes.

1-Sample t-Test of True Mean vs. Action Level



Statistical Assumptions

The assumptions associated with the formulas for computing the number of samples are:

- 1. the sample mean is normally distributed (this happens if the data are roughly symmetric and the sample size is 30 or more; for skewed data sets, additional samples are required for the sample mean to be normally distributed),
- 2. the variance estimate, S^2 , is reasonable and representative of the population being sampled,
- 3. the population values are not spatially or temporally correlated, and
- the sampling locations will be selected randomly.

The first three assumptions will be assessed in a post data collection analysis. The last assumption is valid because the sample locations were selected using a random process.

Sensitivity Analysis

The sensitivity of the calculation of number of samples was explored by varying the standard deviation, lower bound of gray region (% of action level), beta (%), probability of mistakenly concluding that μ > action level and alpha (%), probability of mistakenly concluding that μ < action level and examining the resulting changes in the number of samples. The following table shows the results of this analysis.

	Number of Samples						
AL 6F0	1 0	α=	=5	α=	:10	α=	:15
AL=652	1.2	s=6658.8	s=3329.4	s=6658.8	s=3329.4	s=6658.8	s=3329.4
	β=5	1130	284	894	225	751	188
LBGR=90	β=10	895	225	686	173	561	141
	β=15	751	189	562	141	449	113
	β=5	284	72	225	57	188	48
LBGR=80	β=10	225	58	173	44	141	36
	β=15	189	49	141	36	113	29
LBGR=70	β=5	127	33	101	26	84	22

β=10	101	27	77	20	63	17
β=15	85	23	64	17	51	13

s = Standard Deviation

LBGR = Lower Bound of Gray Region (% of Action Level)

 β = Beta (%), Probability of mistakenly concluding that μ > action level

 α = Alpha (%), Probability of mistakenly concluding that μ < action level

AL = Action Level (Threshold)

Cost of Sampling

The total cost of the completed sampling program depends on several cost inputs, some of which are fixed, and others that are based on the number of samples collected and measured. Based on the numbers of samples determined above, the estimated total cost of sampling and analysis at this site is \$3,000.00, which averages out to a per sample cost of \$750.00. The following table summarizes the inputs and resulting cost estimates.

COST INFORMATION							
Cost Details	Per Analysis	Per Sample	4 Samples				
Field collection costs		\$100.00	\$400.00				
Analytical costs	\$400.00	\$400.00	\$1,600.00				
Sum of Field & Analytical costs		\$500.00	\$2,000.00				
Fixed planning and validation costs			\$1,000.00				
Total cost			\$3,000.00				

Data Analysis

The following data points were entered by the user for analysis.

Rank	1	2	3	4	5	6	7	8	9	10
0	0	648	747	748	790	858	915	917	959	1090
10	1110	1130	1160	1200	1240	1390	1495	1760	1770	1830
20	1960	2140	2250	2460	2480	2800	3310	3510	3630	3640
30	4180	4660	5140	5140	5880	6880	7640	7690	8450	9150
40	1.09e+004	1.14e+004	1.38e+004							

SUMMARY STATISTICS						
n	43					
Min	0					
Max	13800					
Range	13800					
Mean	3508.1					
Median	2140					
Variance	1.1121e+007					
StdDev	3334.8					
Std Error	508.56					
Skewness	1.4617					
Interquartile Range	4030					

	Percentiles							
1%	1% 5% 10% 25% 50% 75% 90% 95% 99%							99%
0	667.8	764.8	1110	2140	5140	8870	1.13e+004	1.38e+004

Outlier Test

Rosner's test for multiple outliers was performed to test whether the most extreme value is a statistical outlier. The test was conducted at the 5% significance level.

Data should not be excluded from analysis solely on the basis of the results of this or any other statistical test. If any values are flagged as possible outliers, further investigation is recommended to determine whether there is a plausible explanation that justifies removing or replacing them.

In using Rosner's test to detect up to 1 outlier, a test statistic R_1 is calculated, and compared with a critical value C_1 to test the hypothesis that there is one outlier in the data.

	ROSNER'S OUTLIER TEST								
k	k Test Statistic R _k 5% Critical Value C _k Significant?								
1	3.066	3.06	Yes						

The test statistic 3.066 exceeded the corresponding critical value, therefore that test is significant and we conclude that the most extreme value is an outlier at the 5% significance level.

SUSPECTED OUTLIERS	
1	13800

A normal distribution test indicated that the data do not appear to be normally distributed, so further investigation is recommended before using the results of this test. Because Rosner's test can be used only when the data without the suspected outlier are approximately normally distributed, a Shapiro-Wilk test for normality was performed at a 5% significance level.

NORMAL DISTRIBUTION TEST (excluding outliers)		
Shapiro-Wilk Test Statistic	0.8126	
Shapiro-Wilk 5% Critical Value	0.941	

The calculated Shapiro-Wilk test statistic is less than the 5% Shapiro-Wilk critical value, so the test rejects the hypothesis that the data are normal and concludes that the data, excluding the most extreme value, do not appear to follow a normal distribution at the 5% level of significance. Rosner's test may not be appropriate if the assumption of normally distributed data is not justified for this data set. Examine the Q-Q plot displayed below to further assess the normality of the data.

Data Plots

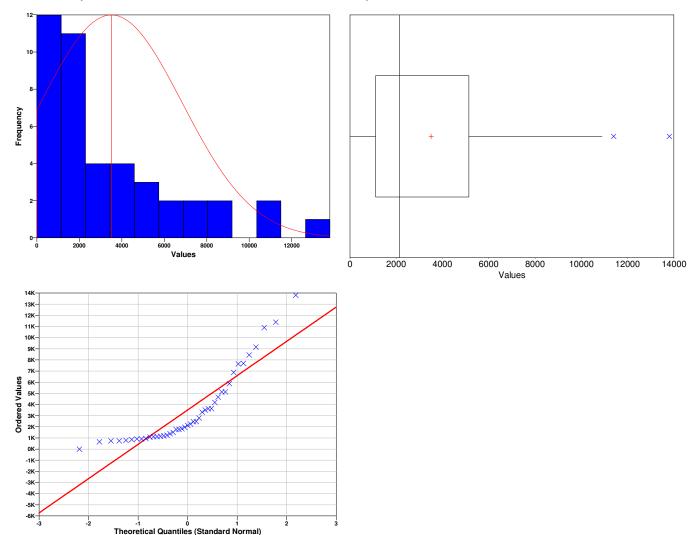
Graphical displays of the data are shown below.

The Histogram is a plot of the fraction of the n observed data that fall within specified data "bins." A histogram is generated by dividing the x axis (range of the observed data values) into "bins" and displaying the number of data in each bin as the height of a bar for the bin. The area of the bar is the fraction of the n data values that lie within the bin. The sum of the fractions for all bins equals one. A histogram is used to assess how the n data are distributed (spread) over their range of values. If the histogram is more or less symmetric and bell shaped, then the data may be normally distributed.

The Box and Whiskers plot is composed of a central box divided by a line, and with two lines extending out from the box, called the "whiskers". The line through the box is drawn at the median of the n data observed. The two ends of the box represent the 25th and 75th percentiles of the n data values, which are also called the lower and upper quartiles, respectively, of the data set. The sample mean (mean of the n data) is shown as a "+" sign. The upper whisker extends to the largest data value that is less than the upper quartile plus 1.5 times the interquartile range (upper quartile minus the lower quartile). The lower whisker extends to the smallest data value that is greater than the lower quartile minus 1.5

times the interquartile range. Extreme data values (greater or smaller than the ends of the whiskers) are plotted individually as blue Xs. A Box and Whiskers plot is used to assess the symmetry of the distribution of the data set. If the distribution is symmetrical, the box is divided into two equal halves by the median, the whiskers will be the same length, and the number of extreme data points will be distributed equally on either end of the plot.

The Q-Q plot graphs the quantiles of a set of n data against the quantiles of a specific distribution. We show here only the Q-Q plot for an assumed normal distribution. The p^{th} quantile of a distribution of data is the data value, x_n , for which a fraction p of the distribution is less than x_n . If the data plotted on the normal distribution Q-Q plot closely follow a straight line, even at the ends of the line, then the data may be assumed to be normally distributed. If the data points deviate substantially from a linear line, then the data are not normally distributed.



For more information on these plots consult Guidance for Data Quality Assessment, EPA QA/G-9, pgs 2.3-1 through 2.3-12. (http://www.epa.gov/quality/ga-docs.html).

Tests

A goodness-of-fit test was performed to test whether the data set had been drawn from an underlying normal distribution. The Shapiro-Wilk (SW) test was used to test the null hypothesis that the data are normally distributed. The test was conducted at the 5% significance level, i.e., the probability the test incorrectly rejects the null hypothesis was set at 0.05.

NORMAL DISTRIBUTION TEST		
Shapiro-Wilk Test Statistic	0.816	
Shapiro-Wilk 5% Critical Value	0.943	

The calculated SW test statistic is less than the 5% Shapiro-Wilk critical value, so we can reject the hypothesis that the

data are normal, or in other words the data do not appear to follow a normal distribution at the 5% level of significance. The Q-Q plot displayed above should be used to further assess the normality of the data.

Upper Confidence Limit on the True Mean

Two methods were used to compute the upper confidence limit (UCL) on the mean. The first is a parametric method that assumes a normal distribution. The second is the Chebyshev method, which requires no distributional assumption.

UCLs ON THE MEAN	
95% Parametric UCL	4363
95% Non-Parametric (Chebyshev) UCL	5725

Because the data do not appear to be normally distributed according to the goodness-of-fit test performed above, the non-parametric UCL (5725) may be a more accurate upper confidence limit on the true mean.

One-Sample t-Test

A one-sample t-test was performed to compare the sample mean to the action level. The null hypothesis used is that the true mean equals or exceeds the action level (AL). The t-test was conducted at the 5% significance level. The sample value *t* was computed using the following equation:

$$t = \frac{\bar{x} - AL}{SE}$$

where

x is the sample mean of the n=43 data,

AL is the action level or threshold (6521.2),

SE is the standard error = (standard deviation) / (square root of n).

This t was then compared with the critical value $t_{0.95}$, where $t_{0.95}$ is the value of the t distribution with n-1=42 degrees of freedom for which the proportion of the distribution to the left of $t_{0.95}$ is 0.95. The null hypothesis will be rejected if $t < -t_{0.95}$.

ONE-SAMPLE t-TEST			
t-statistic	Critical Value t _{0.95}	Null Hypothesis	
-5.9249	1.682	Reject	

The test rejected the null hypothesis that the mean value at the site exceeds the threshold, therefore conclude the true mean is less than the threshold.

Because the data do not appear to be normally distributed, the MARSSIM Sign Test might be preferred over the One Sample t-Test. The following table represents the results of the MARSSIM Sign Test using the current data:

MARSSIM Sign Test		
Test Statistic (S+)	95% Critical Value	Null Hypothesis
35	27	Reject

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